Faculty of Engineering (Shoubra)
Engineering Mathematics and
Physics Department

$3^{\text {rd }}$ Quiz

1) Find $F(s)$ of the following functions:
a) $f(t)=\sin t, t>2, b) \frac{e^{2 t}-e^{-3 t}}{t^{2}}$, c) $f(t)=t+4, f(t+2)=f(t)$
2) Solve the differential equation

$$
y^{\prime \prime}-3 y^{`}+2 y=20 \mathrm{e}^{5 \mathrm{t}}, \quad y(0)=7, y^{\prime}(0)=2
$$

3) Verify
a) $\int_{0}^{\infty} \frac{\mathrm{t}^{\mathrm{ac}-1}}{\left(1+\mathrm{t}^{\mathrm{c}}\right)^{\mathrm{a}+\mathrm{b}}} \mathrm{dt}=\frac{1}{\mathrm{c}} \beta(\mathrm{a}, \mathrm{b})$,
b) $\int_{0}^{1} \frac{\mathrm{t}^{\mathrm{aq}-1}}{\sqrt[q]{\left(1-\mathrm{t}^{\mathrm{q}}\right)}} \mathrm{dt}=\frac{1}{\mathrm{q}} \beta(\mathrm{a}, 1-1 / \mathrm{q})$
